



A Guide to Rigor in Mathematics

In order to provide a quality mathematical education for students, instruction must be rigorous, focused, and coherent. This document provides explanations and a standards-based alignment to assist teachers in providing the first of those: a rigorous education. While this document will help teachers identify the explicit component(s) of rigor called for by each of the Louisiana Student Standards for Mathematics (LSSM), it is up to the teacher to ensure his/her instruction aligns to the expectations of the standards, allowing for the proper development of rigor in the classroom.

This rigor document is considered a “living” document as we believe that teachers and other educators will find ways to improve the document as they use it. Please send feedback to LouisianaStandards@la.gov so that we may use your input when updating this guide.

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Table of Contents

Introduction

Definitions of the Components of Rigor	2
A Special Note on Procedural Skill and Fluency	2
Recognizing the Components of Rigor	3
Focus in the standards	3

Rigor by Grade/Content Level

Kindergarten	4
1st Grade	6
2nd Grade	8
3rd Grade	10
4th Grade	14
5th Grade	18
6th Grade	22
7th Grade	26
8th Grade	30
Algebra I	34
Geometry	38
Algebra II	42

Definitions of the Components of Rigor

Rigorous teaching in mathematics does not simply mean increasing the difficulty or complexity of practice problems. Incorporating rigor into classroom instruction and student learning means exploring at a greater depth, the standards and ideas with which students are grappling. There are **three** components of rigor that will be expanded upon in this document, and each is equally important to student mastery: **Conceptual Understanding, Procedural Skill and Fluency, and Application.**

- **Conceptual Understanding** refers to understanding mathematical concepts, operations, and relations. It is more than knowing isolated facts and methods. Students should be able to make sense of why a mathematical idea is important and the kinds of contexts in which it is useful. It also allows students to connect prior knowledge to new ideas and concepts.
- **Procedural Skill and Fluency** is the ability to apply procedures accurately, efficiently, and flexibly. It requires speed and accuracy in calculation while giving students opportunities to practice basic skills. Students' ability to solve more complex application tasks is dependent on procedural skill and fluency.
- **Application** provides valuable content for learning and the opportunity to solve problems in a relevant and a meaningful way. It is through real-world application that students learn to select an efficient method to find a solution, determine whether the solution makes sense by reasoning, and develop critical thinking skills.

A Special Note on Procedural Skill and Fluency

While speed is definitely a component of fluency, it is not necessarily speed in producing an answer; rather, fluency can be observed by watching the speed with which a student engages with a particular problem. Furthermore, fluency does not require the most efficient strategy. The standards specify grade-level appropriate strategies or types of strategies with which students should demonstrate fluency (e.g., 1.OA.C.6 allows for students to use counting on, making ten, creating equivalent but easier or known sums, etc.). It should also be noted that teachers should expect some procedures to take longer than others (e.g., fluency with the standard algorithm for division, 6.NS.B.2, as compared to fluently adding and subtracting within 10, 1.OA.C.6).

Standards identified as targeting procedural skill and fluency do not all have an expectation of automaticity and/or rote recall. Only two standards, 2.OA.B.2 and 3.OA.C.7, have explicit expectations of students knowing facts from memory. Other standards targeting procedural skill and fluency do not require students to reach automaticity. For example, in 4.G.A.2, students do not need to reach automaticity in classifying two-dimensional figures.

Recognizing the Components of Rigor

In the LSSM each standard is aligned to one or more components of rigor, meaning that each standard aims to promote student growth in conceptual understanding, procedural skill and fluency, and/or application. Key words and phrases in the standards indicate which component(s) of rigor the standard is targeting: conceptual understanding standards often use terms like *understand*, *recognize*, or *interpret*; procedural skill and fluency standards tend to use words like *fluently*, *find*, or *solve*; and application standards typically use phrases like *word problems* or *real-world problems*. Key words and phrases are underlined in each standard to help clarify the identified component(s) of rigor for each standard.

Focus in the Standards

Not all content in a given grade is emphasized equally in the standards. Some clusters require greater emphasis than others based on the depth of the ideas, the time that they take to master, and/or their importance to future mathematics or the demands of college and career readiness. More time in these areas is also necessary for students to meet the Louisiana Standards for Mathematical Practice. To say that some things have greater emphasis is not to say that anything in the standards can safely be neglected in instruction. Neglecting material will leave gaps in student skill and understanding and may leave students unprepared for the challenges of a later grade. Students should spend the large majority of their time on the major work of the grade (■). Supporting work (■) and, where appropriate, additional work (■) can engage students in the major work of the grade.

Kindergarten

LSSM – Kindergarten		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
K.CC.A.1	<u>Count</u> to 100 by ones and by tens.		✓	
K.CC.A.2	<u>Count</u> forward beginning from a given number within the known sequence (instead of having to begin at 1).		✓	
K.CC.A.3	<u>Write</u> numbers from 0 to 20. <u>Represent</u> a number of objects with a written numeral 0-20 (with 0 representing a count of no objects).	✓		
K.CC.B.4	<u>Understand</u> the relationship between numbers and quantities; connect counting to cardinality.	✓		
K.CC.B.4a	When counting objects in standard order, say the number names as they relate to each object in the group, <u>demonstrating</u> one-to-one correspondence.	✓		
K.CC.B.4b	<u>Understand</u> that the last number name said tells the number of objects counted. The number of objects is the same regardless of their arrangement or the order in which they were counted.	✓		
K.CC.B.4c	<u>Understand</u> that each successive number name refers to a quantity that is one larger.	✓		
K.CC.B.5	<u>Count</u> to answer “How many?” questions.		✓	
K.CC.B.5a	<u>Count</u> objects up to 20, arranged in a line, a rectangular array, or a circle.		✓	
K.CC.B.5b	<u>Count</u> objects up to 10 in a scattered configuration.		✓	
K.CC.B.5c	When given a number from 1-20, <u>count</u> out that many objects.		✓	
K.CC.C.6	<u>Identify</u> whether the number of objects in one group is greater than, less than, or equal to the number of objects in another group, e.g., by using matching and counting strategies.	✓		
K.CC.C.7	<u>Compare</u> two numbers between 1 and 10 presented as written numerals.	✓		
K.OA.A.1	<u>Represent</u> addition and subtraction with objects, fingers, mental images, drawings, sounds (e.g., claps), acting out situations, verbal explanations, expressions, or equations.	✓		
K.OA.A.2	Solve addition and subtraction <u>word problems</u> , and <u>add and subtract</u> within 10, e.g., by using objects or drawings to represent the problem.		✓	✓
K.OA.A.3	<u>Decompose</u> numbers less than or equal to 10 into pairs in more than one way, e.g., by using objects or drawings, and record each decomposition by a drawing or equation (e.g., $5 = 2 + 3$ and $5 = 4 + 1$).	✓		
K.OA.A.4	For any number from 1 to 9, <u>find</u> the number that makes 10 when added to the given number, e.g., by using objects or drawings, and record the answer with a drawing or equation.	✓		
K.OA.A.5	<u>Fluently</u> add and subtract within 5.		✓	
K.NBT.A.1	Gain <u>understanding</u> of place value.	✓		
K.NBT.A.1a	<u>Understand</u> that the numbers 11–19 are composed of ten ones and one, two, three, four, five, six, seven, eight, or nine ones.	✓		

LSSM – Kindergarten		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
K.NBT.A.1a	<u>Understand</u> that the numbers 11–19 are composed of ten ones and one, two, three, four, five, six, seven, eight, or nine ones.	✓		
K.NBT.A.1b	<u>Compose and decompose</u> numbers 11 to 19 using place value (e.g., by using objects or drawings).	✓		
K.NBT.A.1c	<u>Record</u> each composition or decomposition using a drawing or equation (e.g., 18 is one ten and eight ones, $18 = 1 \text{ ten} + 8 \text{ ones}$, $18 = 10 + 8$).	✓		
K.MD.A.1	<u>Describe</u> measurable attributes of objects, such as length or weight. <u>Describe</u> several measurable attributes of a single object.	✓		
K.MD.A.2	Directly <u>compare</u> two objects with a measurable attribute in common, to see which object has “more of”/“less of” the attribute, and <u>describe</u> the difference. <i>For example, directly compare the heights of two children and describe one child as taller/shorter.</i>	✓		
K.MD.B.3	<u>Classify</u> objects into given categories based on their attributes; <u>count</u> the numbers of objects in each category and <u>sort</u> the categories by count.	✓	✓	
K.MD.C.4	<u>Recognize</u> pennies, nickels, dimes, and quarters by name and value (e.g., This is a nickel and it is worth 5 cents.)	✓		
K.G.A.1	<u>Describe</u> objects in the <u>environment</u> using names of shapes, and <u>describe</u> the relative positions of these objects using terms such as above, below, beside, in front of, behind, and next to.	✓		✓
K.G.A.2	Correctly <u>name</u> shapes regardless of their orientations or overall size.	✓		
K.G.A.3	<u>Identify</u> shapes as two-dimensional (lying in a plane, “flat”) or three-dimensional (“solid”).	✓		
K.G.B.4	<u>Analyze and compare</u> two- and three-dimensional shapes, in different sizes and orientations, using informal language to describe their similarities, differences, parts (e.g., number of sides and vertices/“corners”) and other attributes (e.g., having sides of equal length).	✓		
K.G.B.5	<u>Model</u> shapes in the world by building shapes from components (e.g., sticks and clay balls) and drawing shapes.	✓		
K.G.B.6	<u>Compose</u> simple shapes to form larger shapes. <i>For example, “Can you join these two triangles with full sides touching to make a rectangle?”</i>	✓		

1st Grade

LSSM – 1 st Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
1.OA.A.1	Use addition and subtraction within 20 to solve <u>word problems</u> involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.			✓
1.OA.A.2	Solve <u>word problems</u> that call for addition of three whole numbers whose sum is less than or equal to 20, e.g., by using objects, drawings, and equations with a symbol for the unknown number to represent the problem.			✓
1.OA.B.3	<u>Apply properties of operations</u> to add and subtract. Examples: If $8 + 3 = 11$ is known, then $3 + 8 = 11$ is also known. (Commutative property of addition.) To add $2 + 6 + 4$, the second two numbers can be added to make a ten, so $2 + 6 + 4 = 2 + 10 = 12$. (Associative property of addition.)	✓		
1.OA.B.4	<u>Understand</u> subtraction as an unknown-addend problem. <i>For example, subtract $10 - 8$ by finding the number that makes 10 when added to 8.</i>	✓		
1.OA.C.5	<u>Relate</u> counting to addition and subtraction (e.g., by counting on 2 to add 2).	✓		
1.OA.C.6	Add and subtract within 20, <u>demonstrating fluency</u> for addition and subtraction within 10. <u>Use strategies</u> such as counting on; making ten (e.g., $8 + 6 = 8 + 2 + 4 = 10 + 4 = 14$); decomposing a number leading to a ten (e.g., $13 - 4 = 13 - 3 - 1 = 10 - 1 = 9$); using the relationship between addition and subtraction (e.g., knowing that $8 + 4 = 12$, one knows $12 - 8 = 4$); and creating equivalent but easier or known sums (e.g., adding $6 + 7$ by creating the known equivalent $6 + 6 + 1 = 12 + 1 = 13$).	✓	✓	
1.OA.D.7	<u>Understand</u> the meaning of the equal sign, and <u>determine</u> if equations involving addition and subtraction are true or false. <i>For example, which of the following equations are true and which are false? $6 = 6$, $7 = 8 - 1$, $5 + 2 = 2 + 5$, $4 + 1 = 5 + 2$.</i>	✓	✓	
1.OA.D.8	<u>Determine</u> the unknown whole number in an addition or subtraction equation relating three whole numbers. <i>For example, determine the unknown number that makes the equation true in each of the equations $8 + ? = 11$, $5 = ? - 3$, $6 + 6 = ?$.</i>		✓	
1.NBT.A.1	<u>Count</u> to 120, starting at any number less than 120. In this range, <u>read and write numerals</u> and <u>represent</u> a number of objects with a written numeral.	✓	✓	
1.NBT.B.2	<u>Understand</u> that the two digits of a two-digit number represent amounts of tens and ones. <u>Understand</u> the following as special cases:	✓		
1.NBT.B.2a	10 can be thought of as a bundle of ten ones — called a “ten.”	✓		
1.NBT.B.2b	The numbers from 11 to 19 are composed of a ten and one, two, three, four, five, six, seven, eight, or nine ones.	✓		
1.NBT.B.2c	The numbers 10, 20, 30, 40, 50, 60, 70, 80, 90 refer to one, two, three, four, five, six, seven, eight, or nine tens (and 0 ones).	✓		

LSSM – 1 st Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
1.NBT.B.3	Compare two two-digit numbers based on meanings of the tens and ones digits, <u>recording</u> the results of comparisons with the symbols $>$, $=$, and $<$.	✓		
1.NBT.C.4	Add within 100, including adding a two-digit number and a one-digit number, and adding a two-digit number and a multiple of 10.	✓		
1.NBT.C.4a	<u>Use</u> concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; <u>relate</u> the strategy to a number sentence; <u>justify</u> the reasoning used with a written explanation.	✓		
1.NBT.C.4b	<u>Understand</u> that in adding two-digit numbers, one adds tens and tens, ones and ones; and sometimes it is necessary to compose a ten.	✓		
1.NBT.C.5	Given a two-digit number, <u>mentally find</u> 10 more or 10 less than the number, without having to count; <u>explain</u> the reasoning used.	✓	✓	
1.NBT.C.6	Subtract multiples of 10 in the range 10-90 from multiples of 10 in the range 10-90 (positive or zero differences), <u>using</u> concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; <u>relate</u> the strategy to a written method and <u>explain</u> the reasoning used.	✓		
1.MD.A.1	<u>Order</u> three objects by length; <u>compare</u> the lengths of two objects indirectly by using a third object.	✓		
1.MD.A.2	<u>Express</u> the length of an object as a whole number of length units, by laying multiple copies of a shorter object (the length unit) end to end; <u>understand</u> that the length measurement of an object is the number of same-size length units that span it with no gaps or overlaps. <i>Limit to contexts where the object being measured is spanned by a whole number of length units with no gaps or overlaps.</i>	✓	✓	
1.MD.B.3	<u>Tell and write</u> time in hours and half-hours using analog and digital clocks.	✓	✓	
1.MD.C.4	<u>Organize, represent, and interpret</u> data with up to three categories; <u>ask and answer</u> questions about the total number of data points, how many in each category, and how many more or less are in one category than in another.	✓	✓	
1.MD.D.5	<u>Determine</u> the value of a collection of coins up to 50 cents. (Pennies, nickels, dimes, and quarters in isolation; not to include a combination of different coins.)		✓	
1.G.A.1	<u>Distinguish</u> between defining attributes (e.g., triangles are closed and three-sided) versus non-defining attributes (e.g., color, orientation, overall size); <u>build and draw</u> shapes to possess defining attributes.	✓		
1.G.A.2	<u>Compose</u> two-dimensional shapes (rectangles, squares, trapezoids, triangles, half-circles, and quarter-circles) and three-dimensional shapes (cubes, right rectangular prisms, right circular cones, and right circular cylinders) to create a composite shape, and <u>compose</u> new shapes from the composite shape.	✓		
1.G.A.3	<u>Partition</u> circles and rectangles into two and four equal shares, <u>describe</u> the shares using the words halves, fourths, and quarters, and use the phrases half of, fourth of, and quarter of. <u>Describe</u> the whole as two of, or four of the shares. <u>Understand</u> for these examples that decomposing into more equal shares creates smaller shares.	✓	✓	

2nd Grade

LSSM – 2 nd Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
2.OA.A.1	Use addition and subtraction within 100 to solve one- and two-step <u>word problems</u> involving situations of adding to, taking from, putting together, taking apart, and comparing, with unknowns in all positions, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.			✓
2.OA.B.2	<u>Fluently</u> add and subtract within 20 using mental strategies. By end of Grade 2, know from memory all sums of two one-digit numbers.		✓	
2.OA.C.3	<u>Determine</u> whether a group of objects (up to 20) has an odd or even number of members, e.g., by pairing objects or counting them by 2s; <u>write</u> an equation to express an even number as a sum of two equal addends.	✓		
2.OA.C.4	<u>Use addition</u> to <u>find</u> the total number of objects arranged in rectangular arrays with up to 5 rows and up to 5 columns; <u>write</u> an equation to express the total as a sum of equal addends.	✓		
2.NBT.A.1	<u>Understand</u> that the three digits of a three-digit number represent amounts of hundreds, tens, and ones; e.g., 706 equals 7 hundreds, 0 tens, and 6 ones. Understand the following as special cases:	✓		
2.NBT.A.1a	100 can be thought of as a bundle of ten tens — called a “hundred.”	✓		
2.NBT.A.1b	The numbers 100, 200, 300, 400, 500, 600, 700, 800, 900 refer to one, two, three, four, five, six, seven, eight, or nine hundreds (and 0 tens and 0 ones).	✓		
2.NBT.A.2	<u>Count</u> within 1000; <u>skip-count</u> by 5s, 10s, and 100s.		✓	
2.NBT.A.3	<u>Read and write</u> numbers to 1000 using base-ten numerals, number names, and expanded form.	✓		
2.NBT.A.4	<u>Compare</u> two three-digit numbers based on meanings of the hundreds, tens, and ones digits, using $>$, $=$, and $<$ symbols to record the results of comparisons.	✓		
2.NBT.B.5	<u>Fluently</u> add and subtract within 100 using strategies based on place value, properties of operations, and/or the relationship between addition and subtraction.		✓	
2.NBT.B.6	Add up to four two-digit numbers <u>using strategies</u> based on place value and properties of operations.	✓		
2.NBT.B.7	Add and subtract within 1000, <u>using</u> concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; <u>justify</u> the reasoning used with a written explanation. <u>Understand</u> that in adding or subtracting three- digit numbers, one adds or subtracts hundreds and hundreds, tens and tens, ones and ones; and sometimes it is necessary to compose or decompose tens or hundreds.	✓		
2.NBT.B.8	<u>Mentally add</u> 10 or 100 to a given number 100–900, and <u>mentally subtract</u> 10 or 100 from a given number 100–900.		✓	

LSSM – 2 nd Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
2.NBT.B.9	<u>Explain</u> why addition and subtraction strategies work, using place value and the properties of operations.	✓		
2.MD.A.1	<u>Measure</u> the length of an object by selecting and using appropriate tools such as rulers, yardsticks, meter sticks, and measuring tapes.		✓	
2.MD.A.2	<u>Measure</u> the length of an object twice, using length units of different lengths for the two measurements; <u>describe</u> how the two measurements relate to the size of the unit chosen.	✓	✓	
2.MD.A.3	<u>Estimate</u> lengths using units of inches, feet, centimeters, and meters.	✓		
2.MD.A.4	<u>Measure</u> to determine how much longer one object is than another, expressing the length difference in terms of a standard length unit.		✓	
2.MD.B.5	Use addition and subtraction within 100 to solve <u>word problems</u> involving lengths that are given in the same units, e.g., by using drawings (such as drawings of rulers) and equations with a symbol for the unknown number to represent the problem.			✓
2.MD.B.6	<u>Represent</u> whole numbers as lengths from 0 on a number line diagram with equally spaced points corresponding to the numbers 0, 1, 2, ..., and <u>represent</u> whole-number sums and differences within 100 on a number line diagram.	✓		
2.MD.C.7	<u>Tell and write</u> time from analog and digital clocks to the nearest five minutes, using a.m. and p.m.	✓	✓	
2.MD.C.8	Solve <u>word problems</u> involving dollar bills, quarters, dimes, nickels, and pennies, using \$ and ¢ symbols appropriately. <i>Example: If you have 2 dimes and 3 pennies, how many cents do you have?</i>			✓
2.MD.D.9	Generate measurement data by <u>measuring</u> lengths of several objects to the nearest whole unit, or by <u>making</u> repeated measurements of the same object. Show the measurements by <u>making</u> a line plot, where the horizontal scale is marked off in whole-number units.		✓	
2.MD.D.10	<u>Draw</u> a picture graph and a bar graph (with single-unit scale) to represent a data set with up to four categories. <u>Solve</u> simple put-together, take-apart, and compare problems using information presented in a bar graph.		✓	
2.G.A.1	<u>Recognize and draw</u> shapes having specified attributes, such as a given number of angles or a given number of equal faces. <u>Identify</u> triangles, quadrilaterals, pentagons, hexagons, and cubes.	✓		
2.G.A.2	<u>Partition</u> a rectangle into rows and columns of same-size squares and <u>count</u> to find the total number of them.	✓	✓	
2.G.A.3	<u>Partition</u> circles and rectangles into two, three, or four equal shares, <u>describe</u> the shares using the words halves, thirds, half of, a third of, etc., and <u>describe</u> the whole as two halves, three thirds, four fourths. <u>Recognize</u> that equal shares of identical wholes need not have the same shape.	✓	✓	

3rd Grade

LSSM – 3 rd Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
3.OA.A.1	<u>Interpret</u> products of whole numbers, e.g., interpret 5×7 as the total number of objects in 5 groups of 7 objects each. <i>For example, describe a context in which a total number of objects can be expressed as 5×7.</i>	✓		
3.OA.A.2	<u>Interpret</u> whole-number quotients of whole numbers, e.g., interpret $56 \div 8$ as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each. <i>For example, describe a context in which a number of shares or a number of groups can be expressed as $56 \div 8$</i>	✓		
3.OA.A.3	Use multiplication and division within 100 to solve <u>word problems</u> in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.			✓
3.OA.A.4	<u>Determine</u> the unknown whole number in a multiplication or division equation relating three whole numbers. <i>For example, determine the unknown number that makes the equation true in each of the equations $8 \times ? = 48$, $5 = _ \div 3$, $6 \times 6 = ?$</i>		✓	
3.OA.B.5	<u>Apply properties of operations as strategies</u> to multiply and divide. ² <i>Examples: If $6 \times 4 = 24$ is known, then $4 \times 6 = 24$ is also known. (Commutative property of multiplication.) $3 \times 5 \times 2$ can be found by $3 \times 5 = 15$, then $15 \times 2 = 30$, or by $5 \times 2 = 10$, then $3 \times 10 = 30$. (Associative property of multiplication.) Knowing that $8 \times 5 = 40$ and $8 \times 2 = 16$, one can find 8×7 as $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56$. (Distributive property.)</i>	✓		
3.OA.B.6	<u>Understand</u> division as an unknown-factor problem. <i>For example, find $32 \div 8$ by finding the number that makes 32 when multiplied by 8.</i>	✓		
3.OA.C.7	<u>Fluently multiply and divide</u> within 100, using strategies such as the relationship between multiplication and division (e.g., knowing that $8 \times 5 = 40$, one knows $40 \div 5 = 8$) or properties of operations. By the end of Grade 3, know from memory all products of two one-digit numbers.		✓	
3.OA.D.8	Solve two-step <u>word problems</u> using the four operations. <u>Represent</u> these problems using equations with a letter standing for the unknown quantity. <u>Assess</u> the reasonableness of answers using mental computation and estimation strategies including rounding.	✓		✓
3.OA.D.9	<u>Identify</u> arithmetic patterns (including patterns in the addition table or multiplication table), and <u>explain</u> them using properties of operations. <i>For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.</i>	✓		
3.NBT.A.1	<u>Use place value understanding</u> to round whole numbers to the nearest 10 or 100.	✓		

LSSM – 3 rd Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
3.NBT.A.2	<u>Fluently</u> add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.		✓	
3.NBT.A.3	Multiply one-digit whole numbers by multiples of 10 in the range 10–90 (e.g., 9×80 , 5×60) <u>using</u> strategies based on place value and properties of operations.	✓		
3.NF.A.1	<u>Understand</u> a fraction $1/b$, with denominators 2, 3, 4, 6, and 8, as the quantity formed by 1 part when a whole is partitioned into b equal parts; understand a fraction a/b as the quantity formed by a parts of size $1/b$.	✓		
3.NF.A.2	<u>Understand</u> a fraction with denominators 2, 3, 4, 6, and 8 as a number on the number line; <u>represent</u> fractions on a number line diagram.	✓		
3.NF.A.2a	<u>Represent</u> a fraction $1/b$ on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into b equal parts. <u>Recognize</u> that each part has size $1/b$ and that the endpoint of the part based at 0 locates the number $1/b$ on the number line.	✓		
3.NF.A.2b	<u>Represent</u> a fraction a/b on a number line diagram by marking off a lengths $1/b$ from 0. <u>Recognize</u> that the resulting interval has size a/b and that its endpoint locates the number a/b on the number line.	✓		
3.NF.A.3	<u>Explain</u> equivalence of fractions with denominators 2, 3, 4, 6, and 8 in special cases, and <u>compare</u> fractions by reasoning about their size.	✓		
3.NF.A.3a	<u>Understand</u> two fractions as equivalent (equal) if they are the same size, or the same point on a number line.	✓		
3.NF.A.3b	<u>Recognize and generate</u> simple equivalent fractions, e.g., $1/2 = 2/4$, $4/6 = 2/3$. <u>Explain</u> why the fractions are equivalent, e.g., by using a visual fraction model.	✓		
3.NF.A.3c	<u>Express</u> whole numbers as fractions, and <u>recognize</u> fractions that are equivalent to whole numbers. <i>Examples: Express 3 in the form $3 = 3/1$; recognize that $6/1 = 6$; locate $4/4$ and 1 at the same point of a number line diagram.</i>	✓		
3.NF.A.3d	<u>Compare</u> two fractions with the same numerator or the same denominator by reasoning about their size. <u>Recognize</u> that comparisons are valid only when the two fractions refer to the same whole. <u>Record</u> the results of comparisons with the symbols $>$, $=$, or $<$, and justify the conclusions, e.g., by using a visual fraction model.	✓		
3.MD.A.1	<u>Understand</u> time to the nearest minute.	✓		
3.MD.A.1a	<u>Tell and write</u> time to the nearest minute and <u>measure</u> time intervals in minutes, within 60 minutes, on an analog and digital clock.	✓	✓	
3.MD.A.1b	<u>Calculate</u> elapsed time greater than 60 minutes to the nearest quarter and half hour on a number line diagram.		✓	
3.MD.A.1c	Solve <u>word problems</u> involving addition and subtraction of time intervals in minutes, e.g., by representing the problem on a number line diagram.			✓

LSSM – 3 rd Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
3.MD.A.2	Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and liters (l). Add, subtract, multiply, or divide to solve one-step word problems involving masses or volumes that are given in the same units, e.g., by using drawings (such as a beaker with a measurement scale) to represent the problem.	✓	✓	✓
3.MD.B.3	Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories. Solve one- and two-step “how many more” and “how many less” problems using information presented in scaled bar graphs. For example, draw a bar graph in which each square in the bar graph might represent 5 pets.		✓	
3.MD.B.4	Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by making a line plot, where the horizontal scale is marked off in appropriate units—whole numbers, halves, or quarters.		✓	
3.MD.C.5	Recognize area as an attribute of plane figures and understand concepts of area measurement.	✓		
3.MD.C.5a	A square with side length 1 unit, called “a unit square,” is said to have “one square unit” of area, and can be used to measure area.	✓		
3.MD.C.5b	A plane figure which can be covered without gaps or overlaps by n unit squares is said to have an area of n square units.	✓		
3.MD.C.6	Measure areas by counting unit squares (square cm, square m, square in, square ft, and improvised units).	✓		
3.MD.C.7	Relate area to the operations of multiplication and addition.	✓		
3.MD.C.7a	Find the area of a rectangle with whole-number side lengths by tiling it, and show that the area is the same as would be found by multiplying the side lengths.	✓	✓	
3.MD.C.7b	Multiply side lengths to find areas of rectangles with whole-number side lengths in the context of solving real-world and mathematical problems, and represent whole-number products as rectangular areas in mathematical reasoning.	✓	✓	✓
3.MD.C.7c	Use tiling to show in a concrete case that the area of a rectangle with whole-number side lengths a and b + c is the sum of $a + b$ and $a + c$. Use area models to represent the distributive property in mathematical reasoning.	✓		
3.MD.D.8	Solve real-world and mathematical problems involving perimeters of polygons, including finding the perimeter given the side lengths, finding an unknown side length, and exhibiting rectangles with the same perimeter and different areas or with the same area and different perimeters.		✓	✓
3.MD.E.9	Solve word problems involving pennies, nickels, dimes, quarters, and bills greater than one dollar, using the dollar and cent symbols appropriately.			✓

LSSM – 3 rd Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
3.G.A.1	<u>Understand</u> that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). <u>Recognize</u> rhombuses, rectangles, and squares as examples of quadrilaterals, and <u>draw</u> examples of quadrilaterals that do not belong to any of these subcategories.	✓		
3.G.A.2	<u>Partition</u> shapes into parts with equal areas. <u>Express</u> the area of each part as a unit fraction of the whole. <i>For example, partition a shape into 4 parts with equal area, and describe the area of each part as 1/4 of the area of the shape.</i>	✓	✓	

4th Grade

LSSM – 4 th Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
4.OA.A.1	<u>Interpret</u> a multiplication equation as a comparison and <u>represent</u> verbal statements of multiplicative comparisons as multiplication equations, e.g., interpret $35 = 5 \times 7$ as a statement that 35 is 5 times as many as 7, and 7 times as many as 5.	✓		
4.OA.A.2	Multiply or divide to solve <u>word problems</u> involving multiplicative comparison, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem, distinguishing multiplicative comparison from additive comparison (Example: 6 times as many vs. 6 more than).			✓
4.OA.A.3	Solve multi-step <u>word problems</u> posed with whole numbers and having whole-number answers using the four operations, including problems in which remainders must be interpreted. <u>Represent</u> these problems using equations with a letter standing for the unknown quantity. <u>Assess</u> the reasonableness of answers using mental computation and estimation strategies including rounding. <i>Example: Twenty-five people are going to the movies. Four people fit in each car. How many cars are needed to get all 25 people to the theater at the same time?</i>	✓		✓
4.OA.B.4	Using whole numbers in the range 1–100,			
4.OA.B.4a	<u>Find</u> all factor pairs for a given whole number.		✓	
4.OA.B.4b	<u>Recognize</u> that a given whole number is a multiple of each of its factors.	✓		
4.OA.B.4c	<u>Determine</u> whether a given whole number is a multiple of a given one-digit number.	✓		
4.OA.B.4d	<u>Determine</u> whether a given whole number is prime or composite.	✓		
4.OA.C.5	<u>Generate</u> a number or shape pattern that follows a given rule. <u>Identify</u> apparent features of the pattern that were not explicit in the rule itself. <i>For example, given the rule "Add 3" and the starting number 1, generate terms in the resulting sequence and observe that the terms appear to alternate between odd and even numbers. Explain informally why the numbers will continue to alternate in this way.</i>	✓		
4.NBT.A.1	<u>Recognize</u> that in a multi-digit whole number less than or equal to 1,000,000, a digit in one place represents ten times what it represents in the place to its right. <i>Examples: (1) recognize that $700 \div 70 = 10$; (2) in the number 7,246, the 2 represents 200, but in the number 7,426 the 2 represents 20, recognizing that 200 is ten times as large as 20, by applying concepts of place value and division.</i>	✓		
4.NBT.A.2	<u>Read and write</u> multi-digit whole numbers less than or equal to 1,000,000 using base-ten numerals, number names, and expanded form. <u>Compare</u> two multi-digit numbers based on meanings of the digits in each place, using $>$, $=$, and $<$ symbols to record the results of comparisons.	✓		
4.NBT.A.3	<u>Use place value understanding</u> to round multi-digit whole numbers, less than or equal to 1,000,000, to any place.	✓		
4.NBT.B.4	<u>Fluently</u> add and subtract multi-digit whole numbers, with sums less than or equal to 1,000,000, using the standard algorithm.		✓	

LSSM – 4 th Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
4.NBT.B.5	Multiply a whole number of up to four digits by a one-digit whole number, and multiply two two-digit numbers, <u>using strategies</u> based on place value and the properties of operations. <u>Illustrate and explain</u> the calculation by using equations, rectangular arrays, and/or area models.	✓		
4.NBT.B.6	Find whole-number quotients and remainders with up to four-digit dividends and one-digit divisors, <u>using strategies</u> based on place value, the properties of operations, and/or the relationship between multiplication and division. <u>Illustrate and explain</u> the calculation by using equations, rectangular arrays, and/or area models.	✓		
4.NF.A.1	<u>Explain</u> why a fraction a/b is equivalent to a fraction $(n \times a)/(n \times b)$ by using visual fraction models, with attention to how the number and size of the parts differ even though the two fractions themselves are the same size. <u>Use this principle to recognize and generate</u> equivalent fractions. (Denominators are limited to 2, 3, 4, 5, 6, 8, 10, 12, and 100.)	✓	✓	
4.NF.A.2	<u>Compare</u> two fractions with different numerators and different denominators, e.g., by creating common denominators or numerators, or by comparing to a benchmark fraction such as $1/2$. <u>Recognize</u> that comparisons are valid only when the two fractions refer to the same whole. <u>Record</u> the results of comparisons with symbols $>$, $=$, or $<$, and <u>justify</u> the conclusions, e.g., by using a visual fraction model. (Denominators are limited to 2, 3, 4, 5, 6, 8, 10, 12, and 100.)	✓		
4.NF.B.3	<u>Understand</u> a fraction a/b with $a > 1$ as a sum of fractions $1/b$. (Denominators are limited to 2, 3, 4, 5, 6, 8, 10, 12, and 100.)	✓		
4.NF.B.3a	<u>Understand</u> addition and subtraction of fractions as joining and separating parts referring to the same whole. <i>Example: $3/4 = 1/4 + 1/4 + 1/4$.</i>	✓		
4.NF.B.3b	<u>Decompose</u> a fraction into a sum of fractions with the same denominator in more than one way, <u>recording</u> each decomposition by an equation. <u>Justify</u> decompositions, e.g., by using a visual fraction model. <i>Examples: $3/8 = 1/8 + 1/8 + 1/8$; $3/8 = 1/8 + 2/8$; $2 \frac{1}{8} = 1 + 1 + 1/8 = 8/8 + 8/8 + 1/8$.</i>	✓		
4.NF.B.3c	<u>Add and subtract</u> mixed numbers with like denominators, e.g., by replacing each mixed number with an equivalent fraction, and/or by using properties of operations and the relationship between addition and subtraction.		✓	
4.NF.B.3d	Solve <u>word problems</u> involving addition and subtraction of fractions referring to the same whole and having like denominators, e.g., by using visual fraction models and equations to represent the problem.			✓
4.NF.B.4	<u>Multiply</u> a fraction by a whole number. (Denominators are limited to 2, 3, 4, 5, 6, 8, 10, 12, and 100.)		✓	
4.NF.B.4a	<u>Understand</u> a fraction a/b as a multiple of $1/b$. <i>For example, use a visual fraction model to represent $5/4$ as the product $5 \times (1/4)$, recording the conclusion by the equation $5/4 = 5 \times (1/4)$.</i>	✓		
4.NF.B.4b	<u>Understand</u> a multiple of a/b as a multiple of $1/b$, and <u>use this understanding</u> to multiply a fraction by a whole number. <i>For example, use a visual fraction model to express $3 \times (2/5)$ as $6 \times (1/5)$, recognizing this product as $6/5$. (In general, $n \times (a/b) = (n \times a)/b$.)</i>	✓		
4.NF.B.4c	Solve <u>word problems</u> involving multiplication of a fraction by a whole number, e.g., by using visual fraction models and equations to represent the problem. <i>For example, if each person at a party will eat $3/8$ of a pound of roast beef, and there will be 5 people at the party, how many pounds of roast beef will</i>			✓

LSSM – 4 th Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
	<i>be needed? Between what two whole numbers does your answer lie?</i>			
4.NF.C.5	Express a fraction with denominator 10 as an equivalent fraction with denominator 100, and use this technique to add two fractions with respective denominators 10 and 100. For example, express $\frac{3}{10}$ as $\frac{30}{100}$, and add $\frac{3}{10} + \frac{4}{100} = \frac{34}{100}$.	✓		
4.NF.C.6	Use decimal notation for fractions with denominators 10 or 100. For example, rewrite $\frac{62}{100}$; describe a length as 0.62 meters; locate 0.62 on a number line diagram; represent $\frac{62}{100}$ of a dollar as \$0.62.	✓		
4.NF.C.7	Compare two decimals to hundredths by reasoning about their size. Recognize that comparisons are valid only when the two decimals refer to the same whole. Record the results of comparisons with the symbols $>$, $=$, or $<$, and justify the conclusions, e.g., by using a visual model.	✓		
4.MD.A.1	Know relative sizes of measurement units within one system of units including: ft, in; km, m, cm; kg, g; lb, oz.; l, ml; hr, min, sec. Within a single system of measurement, express measurements in a larger unit in terms of a smaller unit. (Conversions are limited to one-step conversions.) Record measurement equivalents in a two-column table. For example, know that 1 ft is 12 times as long as 1 in. Express the length of a 4 ft snake as 48 in. Generate a conversion table for feet and inches listing the number pairs (1, 12), (2, 24), (3, 36), ...	✓	✓	
4.MD.A.2	Use the four operations to solve word problems involving distances, intervals of time, liquid volumes, masses of objects, and money, including problems involving whole numbers and/or simple fractions (addition and subtraction of fractions with like denominators and multiplying a fraction times a fraction or a whole number), and problems that require expressing measurements given in a larger unit in terms of a smaller unit. Represent measurement quantities using diagrams such as number line diagrams that feature a measurement scale.	✓		✓
4.MD.A.3	Apply the area and perimeter formulas for rectangles in real-world and mathematical problems. For example, find the width of a rectangular room given the area of the flooring and the length, by viewing the area formula as a multiplication equation with an unknown factor.		✓	✓
4.MD.B.4	Make a line plot to display a data set of measurements in fractions of a unit ($\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{8}$). Solve problems involving addition and subtraction of fractions by using information presented in line plots. For example, from a line plot find and interpret the difference in length between the longest and shortest specimens in an insect collection.		✓	
4.MD.C.5	Recognize angles as geometric shapes that are formed wherever two rays share a common endpoint, and understand concepts of angle measurement.	✓		
4.MD.C.5a	An angle is measured with reference to a circle with its center at the common endpoint of the rays, by considering the fraction of the circular arc between the points where the two rays intersect the circle	✓		

LSSM – 4 th Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
4.MD.C.5b	An angle that turns through $\frac{1}{360}$ of a circle is called a "one-degree angle," and can be used to measure angles.	✓		
4.MD.C.5c	An angle that turns through n one-degree angles is said to have an angle measure of n degrees.	✓		
4.MD.C.6	<u>Measure</u> angles in whole-number degrees using a protractor. <u>Sketch</u> angles of specified measure.	✓	✓	
4.MD.C.7	<u>Recognize</u> angle measure as additive. When an angle is decomposed into non-overlapping parts, the angle measure of the whole is the sum of the angle measures of the parts. Solve addition and subtraction problems to find unknown angles on a diagram in <u>real-world and mathematical problems</u> , e.g., by using an equation with a letter for the unknown angle measure.	✓	✓	✓
4.MD.D.8	<u>Recognize</u> area as additive. Find areas of rectilinear figures <u>by decomposing</u> them into non-overlapping rectangles and <u>adding</u> the areas of the non-overlapping parts, applying this technique to solve <u>real-world problems</u> .	✓	✓	✓
4.G.A.1	<u>Draw</u> points, lines, line segments, rays, angles (right, acute, obtuse), and perpendicular and parallel lines. <u>Identify</u> these in two-dimensional figures.	✓		
4.G.A.2	<u>Classify</u> two-dimensional figures based on the presence or absence of parallel or perpendicular lines, or the presence or absence of angles of a specified size. <u>Recognize</u> right triangles as a category, and identify right triangles	✓		
4.G.A.3	<u>Recognize</u> a line of symmetry for a two-dimensional figure as a line across the figure such that the figure can be folded along the line into matching parts. <u>Identify</u> line-symmetric figures and <u>draw</u> lines of symmetry.	✓		

5th Grade

LSSM – 5 th Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
5.OA.A.1	Use parentheses or brackets in numerical expressions, and <u>evaluate</u> expressions with these symbols.	✓	✓	
5.OA.A.2	<u>Write</u> simple expressions that record calculations with whole numbers, fractions and decimals, and <u>interpret</u> numerical expressions without evaluating them. <i>For example, express the calculation "add 8 and 7, then multiply by 2" as $2 \times (8 + 7)$. Recognize that $3 \times (18,932 + 9.21)$ is three times as large as $18,932 + 9.21$, without having to calculate the indicated sum or product.</i>	✓		
5.OA.B.3	<u>Generate</u> two numerical patterns using two given rules. <u>Identify</u> apparent relationships between corresponding terms. <u>Form</u> ordered pairs consisting of corresponding terms from the two patterns, and <u>graph</u> the ordered pairs on a coordinate plane. <i>For example, given the rule "Add 3" and the starting number 0, and given the rule "Add 6" and the starting number 0, generate terms in the resulting sequences, and observe that the terms in one sequence are twice the corresponding terms in the other sequence. Explain informally why this is so.</i>	✓		
5.NBT.A.1	<u>Recognize</u> that in a multi-digit number, a digit in one place represents 10 times as much as it represents in the place to its right and 1/10 of what it represents in the place to its left.	✓		
5.NBT.A.2	<u>Explain and apply</u> patterns in the number of zeros of the product when multiplying a number by powers of 10. <u>Explain and apply</u> patterns in the values of the digits in the product or the quotient, when a decimal is multiplied or divided by a power of 10. <u>Use</u> whole-number exponents to denote powers of 10. <i>For example, $10^0 = 1$, $10^1 = 10 \dots$ and $2.1 \times 10^2 = 210$.</i>	✓		
5.NBT.A.3	<u>Read, write, and compare</u> decimals to thousandths.	✓		
5.NBT.A.3a	<u>Read and write</u> decimals to thousandths using base-ten numerals, number names, and expanded form, e.g., $347.392 = 3 \times 100 + 4 \times 10 + 7 \times 1 + 3 \times (1/10) + 9 \times (1/100) + 2 \times (1/1000)$.	✓		
5.NBT.A.3b	<u>Compare</u> two decimals to thousandths based on meanings of the digits in each place, using $>$, $=$, and $<$ symbols to record the results of comparisons.	✓		
5.NBT.A.4	<u>Use place value understanding</u> to round decimals to any place.	✓		
5.NBT.B.5	<u>Fluently</u> multiply multi-digit whole numbers using the standard algorithm.		✓	
5.NBT.B.6	Find whole-number quotients of whole numbers with up to four-digit dividends and two-digit divisors, <u>using strategies</u> based on place value, the properties of operations, subtracting multiples of the divisor, and/or the relationship between multiplication and division. <u>Illustrate and/or explain</u> the calculation by using equations, rectangular arrays, area models, or other strategies based on place value.	✓		

LSSM – 5 th Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
5.NBT.B.7	Add, subtract, multiply, and divide decimals to hundredths, <u>using</u> concrete models or drawings and strategies based on place value, properties of operations, and/or the relationship between addition and subtraction; <u>justify</u> the reasoning used with a written explanation.	✓		
5.NF.A.1	<u>Add and subtract</u> fractions with unlike denominators (including mixed numbers) <u>by replacing given fractions with equivalent fractions in such a way as to produce an equivalent sum or difference of fractions with like denominators</u> . For example, $2/3 + 5/4 = 8/12 + 15/12 = 23/12$. (In general, $a/b + c/d = (ad + bc)/bd$.)	✓	✓	
5.NF.A.2	Solve <u>word problems</u> involving addition and subtraction of fractions.			✓
5.NF.A.2a	Solve <u>word problems</u> involving addition and subtraction of fractions referring to the same whole, including cases of unlike denominators, e.g., by using visual fraction models or equations to represent the problem.			✓
5.NF.A.2b	Use benchmark fractions and number sense of fractions to <u>estimate mentally and justify</u> the reasonableness of answers. For example, recognize an incorrect result $2/5 + 1/2 = 3/7$, by observing that $3/7 < 1/2$.	✓		
5.NF.B.3	<u>Interpret</u> a fraction as division of the numerator by the denominator ($a/b = a \div b$). Solve <u>word problems</u> involving division of whole numbers leading to answers in the form of fractions or mixed numbers, e.g., by using visual fraction models or equations to represent the problem. For example, interpret $3/4$ as the result of dividing 3 by 4, noting that $3/4$ multiplied by 4 equals 3, and that when 3 wholes are shared equally among 4 people each person has a share of size $3/4$. If 9 people want to share a 50-pound sack of rice equally by weight, how many pounds of rice should each person get? Between what two whole numbers does your answer lie?	✓		✓
5.NF.B.4	<u>Apply and extend previous understandings</u> of multiplication to multiply a fraction or whole number by a fraction.	✓		
5.NF.B.4a	<u>Interpret</u> the product $(m/n) \times q$ as m parts of a partition of q into n equal parts; equivalently, as the result of a sequence of operations, $m \times q \div n$. For example, use a visual fraction model to show understanding, and create a story context for $(m/n) \times q$.	✓		
5.NF.B.4b	<u>Construct</u> a model to develop understanding of the concept of multiplying two fractions and <u>create</u> a story context for the equation. [In general, $(m/n) \times (c/d) = (mc)/(nd)$.]	✓		
5.NF.B.4c	Find the area of a rectangle with fractional side lengths <u>by tiling</u> it with unit squares of the appropriate unit fraction side lengths, and show that the area is the same as would be found <u>by multiplying</u> the side lengths.	✓	✓	
5.NF.B.4d	<u>Multiply</u> fractional side lengths to find areas of rectangles, and <u>represent</u> fraction products as rectangular areas.	✓	✓	

LSSM – 5 th Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
5.NF.B.5	<u>Interpret</u> multiplication as scaling (resizing)	✓		
5.NF.B.5a	<u>Comparing</u> the size of a product to the size of one factor on the basis of the size of the other factor, without performing the indicated multiplication.	✓		
5.NF.B.5b	<u>Explaining</u> why multiplying a given number by a fraction greater than 1 results in a product greater than the given number (recognizing multiplication by whole numbers greater than 1 as a familiar case).	✓		
5.NF.B.5c	<u>Explaining</u> why multiplying a given number by a fraction less than 1 results in a product smaller than the given number.	✓		
5.NF.B.5d	<u>Relating</u> the principle of fraction equivalence $a/b = (n \times a)/(n \times b)$ to the effect of multiplying a/b by 1.	✓		
5.NF.B.6	Solve <u>real-world problems</u> involving multiplication of fractions and mixed numbers, e.g., by using visual fraction models or equations to represent the problem.			✓
5.NF.B.7	<u>Apply and extend previous understandings</u> of division to divide unit fractions by whole numbers and whole numbers by unit fractions.	✓		
5.NF.B.7a	<u>Interpret</u> division of a unit fraction by a non-zero whole number, and <u>compute</u> such quotients. <i>For example, create a story context for $(1/3) \div 4$, and use a visual fraction model to show the quotient. Use the relationship between multiplication and division to explain that $(1/3) \div 4 = 1/12$ because $(1/12) \times 4 = 1/3$.</i>	✓	✓	
5.NF.B.7b	<u>Interpret</u> division of a whole number by a unit fraction, and <u>compute</u> such quotients. <i>For example, create a story context for $4 \div (1/5)$, and use a visual fraction model to show the quotient. Use the relationship between multiplication and division to explain that $4 \div (1/5) = 20$ because $20 \times (1/5) = 4$.</i>	✓	✓	
5.NF.B.7c	Solve <u>real-world problems</u> involving division of unit fractions by non-zero whole numbers and division of whole numbers by unit fractions, e.g., by using visual fraction models and equations to represent the problem. <i>For example, how much chocolate will each person get if 3 people share $1/2$ lb of chocolate equally? How many $1/3$-cup servings are in 2 cups of raisins?</i>			✓
5.MD.A.1	<u>Convert</u> among different-sized standard measurement units within a given measurement and use these conversions in solving <u>multi-step, real-world problems</u> (e.g., convert 5 cm to 0.05 m; 9 ft to 108 in).		✓	✓
5.MD.B.2	<u>Make</u> a line plot to display a data set of measurements in fractions of a unit ($1/2, 1/4, 1/8$). Use operations on fractions for this grade to <u>solve problems</u> involving information presented in line plots. <i>For example, given different measurements of liquid in identical beakers, find the amount of liquid each beaker would contain if the total amount in all the beakers were redistributed equally.</i>		✓	✓
5.MD.C.3	<u>Recognize</u> volume as an attribute of solid figures and <u>understand</u> concepts of volume measurement.	✓		
5.MD.C.3a	A cube with side length 1 unit, called a "unit cube," is said to have "one cubic unit" of volume, and can be used to measure volume.	✓		
5.MD.C.3b	A solid figure which can be packed without gaps or overlaps using n unit cubes is said to have a volume of n cubic units.	✓		

LSSM – 5 th Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
5.MD.C.4	Measure volumes <u>by counting</u> unit cubes, using cubic cm, cubic in, cubic ft, and improvised units.	✓		
5.MD.C.5	<u>Relate</u> volume to the operations of multiplication and addition and solve <u>real-world and mathematical problems</u> involving volume.	✓	✓	✓
5.MD.C.5a	Find the volume of a right rectangular prism with whole-number side lengths <u>by packing</u> it with unit cubes, and show that the volume is the same as would be found <u>by multiplying</u> the edge lengths, equivalently by multiplying the height by the area of the base. <u>Represent</u> threefold whole-number products as volumes, e.g., to represent the associative property of multiplication.	✓	✓	
5.MD.C.5b	Apply the formulas $V = l \times w \times h$ and $V = b \times h$ for rectangular prisms to find volumes of right rectangular prisms with whole-number edge lengths in the context of solving <u>real-world and mathematical problems</u> .		✓	✓
5.MD.C.5c	<u>Recognize</u> volume as additive. Find volumes of solid figures composed of two non-overlapping right rectangular prisms <u>by adding</u> the volumes of the non-overlapping parts, applying this technique to solve <u>real-world problems</u> .	✓	✓	✓
5.G.A.1	Use a pair of perpendicular number lines, called axes, to <u>define</u> a coordinate system, with the intersection of the lines (the origin) arranged to coincide with the 0 on each line and a given point in the plane located by using an ordered pair of numbers, called its coordinates. <u>Understand</u> that the first number in the ordered pair indicates how far to travel from the origin in the direction of one axis, and the second number in the ordered pair indicates how far to travel in the direction of the second axis, with the convention that the names of the two axes and the coordinates correspond (e.g., x-axis and x-coordinate, y-axis and y-coordinate).	✓		
5.G.A.2	Represent <u>real-world and mathematical problems</u> by graphing points in the first quadrant of the coordinate plane, and <u>interpret</u> coordinate values of points in the context of the situation.	✓	✓	✓
5.G.B.3	<u>Understand</u> that attributes belonging to a category of two-dimensional figures also belong to all subcategories of that category. <i>For example, all rectangles have four right angles and squares are rectangles, so all squares have four right angles.</i>	✓		
5.G.B.4	<u>Classify</u> quadrilaterals in a hierarchy based on properties. (Students will define a trapezoid as a quadrilateral with at least one pair of parallel sides.)	✓		

6th Grade

LSSM – 6 th Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
6.RP.A.1	Understand the concept of a ratio and use ratio language to describe a ratio relationship between two quantities. For example, "The ratio of wings to beaks in the bird house at the zoo was 2:1, because for every 2 wings there was 1 beak." "For every vote candidate A received, candidate C received nearly three votes."	✓		
6.RP.A.2	Understand the concept of a unit rate a/b associated with a ratio $a:b$ with $b \neq 0$, and use rate language in the context of a ratio relationship. For example, "This recipe has a ratio of 3 cups of flour to 4 cups of sugar, so there is $3/4$ cup of flour for each cup of sugar." "We paid \$75 for 15 hamburgers, which is a rate of \$5 per hamburger."	✓		
6.RP.A.3	Use ratio and rate reasoning to solve real-world and mathematical problems, e.g., by reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or equations.	✓	✓	✓
6.RP.A.3a	Make tables of equivalent ratios relating quantities with whole-number measurements, find missing values in the tables, and plot the pairs of values on the coordinate plane. Use tables to compare ratios.	✓	✓	
6.RP.A.3b	Solve unit rate problems including those involving unit pricing and constant speed. For example, if it took 7 hours to mow 4 lawns, then at that rate, how many lawns could be mowed in 35 hours? At what unit rate were lawns being mowed?		✓	✓
6.RP.A.3c	Find a percent of a quantity as a rate per 100 (e.g., 30% of a quantity means $30/100$ times the quantity); solve problems involving finding the whole, given a part and the percent.		✓	✓
6.RP.A.3d	Use ratio reasoning to convert measurement units; manipulate and transform units appropriately when multiplying or dividing quantities.	✓	✓	
6.NS.A.1	Interpret and compute quotients of fractions, and solve word problems involving division of fractions by fractions, e.g., by using visual fraction models and equations to represent the problem. For example, create a story context for $(2/3) \div (3/4)$ and use a visual fraction model to show the quotient; use the relationship between multiplication and division to explain that $(2/3) \div (3/4) = 8/9$ because $3/4$ of $8/9$ is $2/3$. (In general, $(a/b) \div (c/d) = ad/bc$.) How much chocolate will each person get if 3 people share $1/2$ lb of chocolate equally? How many $3/4$ -cup servings are in $2/3$ of a cup of yogurt? How wide is a rectangular strip of land with length $3/4$ mi and area $1/2$ square mi?.	✓	✓	✓
6.NS.B.2	Fluently divide multi-digit numbers using the standard algorithm.		✓	
6.NS.B.3	Fluently add, subtract, multiply, and divide multi-digit decimals using the standard algorithm for each operation.		✓	
6.NS.B.4	Find the greatest common factor of two whole numbers less than or equal to 100 and the least common multiple of two whole numbers less than or equal to 12. Use the distributive property to express a sum of two whole numbers 1-100 with a common factor as a multiple of a sum of two whole numbers with no common factor. For example, express $36 + 8$ as $4(9 + 2)$.	✓	✓	

LSSM – 6 th Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
6.NS.C.5	<u>Understand</u> that positive and negative numbers are used together to describe quantities having opposite directions or values (e.g., temperature above/below zero, elevation above/below sea level, credits/debits, positive/negative electric charge); use positive and negative numbers to <u>represent</u> quantities in real-world contexts, <u>explaining</u> the meaning of 0 in each situation.	✓		
6.NS.C.6	<u>Understand</u> a rational number as a point on the number line. Extend number line diagrams and coordinate axes familiar from previous grades to <u>represent</u> points on the line and in the plane with negative number coordinates.	✓		
6.NS.C.6a	<u>Recognize</u> opposite signs of numbers as indicating locations on opposite sides of 0 on the number line; <u>recognize</u> that the opposite of the opposite of a number is the number itself, e.g., $-(-3) = 3$, and that 0 is its own opposite.	✓		
6.NS.C.6b	<u>Understand</u> signs of numbers in ordered pairs as indicating locations in quadrants of the coordinate plane; <u>recognize</u> that when two ordered pairs differ only by signs, the locations of the points are related by reflections across one or both axes.	✓		
6.NS.C.6c	<u>Find and position</u> integers and other rational numbers on a horizontal or vertical number line diagram; <u>find and position</u> pairs of integers and other rational numbers on a coordinate plane.	✓		
6.NS.C.7	<u>Understand</u> ordering and absolute value of rational numbers.	✓		
6.NS.C.7a	<u>Interpret</u> statements of inequality as statements about the relative position of two numbers on a number line diagram. <i>For example, interpret $-3 > -7$ as a statement that -3 is located to the right of -7 on a number line oriented from left to right.</i>	✓		
6.NS.C.7b	<u>Write, interpret, and explain</u> statements of order for rational numbers in real-world contexts. <i>For example, write $-3^{\circ}\text{C} > -7^{\circ}\text{C}$ to express the fact that -3°C is warmer than -7°C.</i>	✓		
6.NS.C.7c	<u>Understand</u> the absolute value of a rational number as its distance from 0 on the number line; <u>interpret</u> absolute value as magnitude for a positive or negative quantity in a real-world situation. <i>For example, for an account balance of -30 dollars, write $-30 = 30$ to describe the size of the debt in dollars.</i>	✓		
6.NS.C.7d	<u>Distinguish</u> comparisons of absolute value from statements about order. <i>For example, recognize that an account balance less than -30 dollars represents a debt greater than 30 dollars.</i>	✓		
6.NS.C.8	Solve <u>real-world and mathematical problems</u> by graphing points in all four quadrants of the coordinate plane. Include use of coordinates and absolute value to find distances between points with the same first coordinate or the same second coordinate.		✓	✓
6.EE.A.1	<u>Write and evaluate</u> numerical expressions involving whole-number exponents.	✓	✓	
6.EE.A.2	<u>Write, read, and evaluate</u> expressions in which letters stand for numbers.	✓	✓	
6.EE.A.2a	<u>Write</u> expressions that record operations with numbers and with letters standing for numbers. <i>For example, express the calculation "Subtract y from 5" as $5 - y$.</i>	✓		

LSSM – 6 th Grade		Explicit Component(s) of Rigor		
Code	Standard	Conceptual Understanding	Procedural Skill and Fluency	Application
6.EE.A.2b	Identify parts of an expression using mathematical terms (sum, term, product, factor, quotient, coefficient); <u>view</u> one or more parts of an expression as a single entity. For example, describe the expression $2(8 + 7)$ as a product of two factors; view $(8 + 7)$ as both a single entity and a sum of two terms.	✓		
6.EE.A.2c	<u>Evaluate</u> expressions at specific values of their variables. Include expressions that arise from formulas used in real-world problems. <u>Perform</u> arithmetic operations, including those involving whole-number exponents, in the conventional order when there are no parentheses to specify a particular order (Order of Operations). For example, use the formulas $V = s^3$ and $A = 6s^2$ to find the volume and surface area of a cube with sides of length $s = 1/2$.		✓	
6.EE.A.3	<u>Apply</u> the properties of operations to generate equivalent expressions. For example, apply the distributive property to the expression $3(2 + x)$ to produce the equivalent expression $6 + 3x$; apply the distributive property to the expression $24x + 18y$ to produce the equivalent expression $6(4x + 3y)$; apply properties of operations to $y + y + y$ to produce the equivalent expression $3y$.	✓		
6.EE.A.4	<u>Identify</u> when two expressions are equivalent (i.e., when the two expressions name the same number regardless of which value is substituted into them). For example, the expressions $y + y + y$ and $3y$ are equivalent because they name the same number regardless of which number y stands for.	✓		
6.EE.B.5	<u>Understand</u> solving an equation or inequality as a process of answering a question: which values from a specified set, if any, make the equation or inequality true? <u>Use substitution</u> to determine whether a given number in a specified set makes an equation or inequality true.	✓	✓	
6.EE.B.6	Use variables to represent numbers and write expressions when solving a <u>real-world or mathematical problem</u> ; <u>understand</u> that a variable can represent an unknown number, or, depending on the purpose at hand, any number in a specified set.	✓	✓	✓
6.EE.B.7	Solve <u>real-world and mathematical problems</u> by writing and solving equations and inequalities of the form $x + p = q$ and $px = q$ for cases in which p , q and x are all nonnegative rational numbers. Inequalities will include $<$, $>$, \leq , and \geq .		✓	✓
6.EE.B.8	Write an inequality of the form $x > c$ or $x < c$ to represent a constraint or condition in a <u>real-world or mathematical problem</u> . <u>Recognize</u> that inequalities of the form $x > c$ or $x < c$ have infinitely many solutions; <u>represent</u> solutions of such inequalities on number line diagrams.	✓	✓	✓
6.EE.C.9	Use variables to represent two quantities in a <u>real-world problem</u> that change in relationship to one another; <u>write</u> an equation to express one quantity, thought of as the dependent variable, in terms of the other quantity, thought of as the independent variable. <u>Analyze</u> the relationship between the dependent and independent variables using graphs and tables, and <u>relate</u> these to the equation. For example, in a problem involving motion at constant speed, list and graph ordered pairs of distances and times, and write the equation $d = 65t$ to represent the relationship between distance and time.	✓		✓
6.G.A.1	Find the area of right triangles, other triangles, special quadrilaterals, and polygons <u>by composing</u> into rectangles or <u>decomposing</u> into triangles and other shapes; apply these techniques in the context of solving <u>real-world and mathematical problems</u> .	✓	✓	✓